

Multiplying and Simplifying Radicals



EXAMPLE: Perform the following multiplication: $\sqrt[3]{x} \cdot \sqrt[4]{x}$.

SOLUTION:



The **key step** when the indices of the radicals are different is to write the expressions with rational exponents.

$$\begin{aligned}
 \sqrt[3]{x} \cdot \sqrt[4]{x} &= x^{1/3} \cdot x^{1/4} && \text{(write with rational exponents)} \\
 &= x^{1/3 + 1/4} && \text{(use a property of exponents)} \\
 &= x^{4/12 + 3/12} && \text{(create a common denominator for the exponent)} \\
 &= x^{7/12} && \text{(use another property of exponents)} \\
 &= \sqrt[12]{x^7} && \text{(write final answer in radical form to agree with original expression)}
 \end{aligned}$$



Try these yourself and check your answers.

Perform the indicated multiplication, and simplify completely.

a. $\sqrt{t} \cdot \sqrt[8]{t^3}$

b. $\sqrt[3]{2p^2} \cdot \sqrt{3p}$

SOLUTIONS:

a.
$$\begin{aligned}
 \sqrt{t} \cdot \sqrt[8]{t^3} &= t^{1/2} \cdot t^{3/8} && \text{(write with rational exponents)} \\
 &= t^{1/2 + 3/8} && \text{(use a property of exponents)} \\
 &= t^{4/8 + 3/8} && \text{(create a common denominator for the exponents)} \\
 &= t^{7/8} && \text{(use another property of exponents)} \\
 &= \sqrt[8]{t^7} && \text{(write final answer in radical notation to agree with the original expression)}
 \end{aligned}$$

b.
$$\begin{aligned}
 \sqrt[3]{2p^2} \cdot \sqrt{3p} &= (2p^2)^{1/3} \cdot (3p)^{1/2} && \text{(write with rational exponents)} \\
 &= (2p^2)^{2/6} \cdot (3p)^{3/6} && \text{(create a common denominator for the exponents)} \\
 &= \left((2p^2)^2 \right)^{1/6} \left((3p)^3 \right)^{1/6} \\
 &= (4p^4 \cdot 27p^3)^{1/6} \\
 &= (108p^7)^{1/6} \\
 &= \sqrt[6]{108p^7} \\
 &= \sqrt[6]{108p^6 p} \\
 &= p \cdot \sqrt[6]{108p}
 \end{aligned}$$

TRY.

$$\sqrt{24} \cdot \sqrt[4]{8}$$

$$\sqrt[5]{x} \cdot \sqrt{x}$$

$$\sqrt{x^3 y} \cdot \sqrt[3]{xy}$$